

Role of π -Bonding for Trigonal Level Splittings in Chromium(III) Complexes. 4. Doublet States and Zeeman Level Splittings in $[\text{Cr}(\text{bpy})_3]^{3+}$ †

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A detailed analysis of Zeeman splittings of highly resolved spin-forbidden transitions in $[\text{Cr}(\text{bpy})_3](\text{PF}_6)_3$ is presented. Assignments of vibronic bands are made based on low-temperature absorption, emission, and infrared spectra. The pattern of doublet states, obtained for $H = 0$ and $H = 5$ T, is consistent with angular overlap model (AOM) calculations, which allow one to consider σ - and π -interactions between the metal-d and relevant ligand orbitals and the particular angular geometry of the chromophore simultaneously. The observed level splittings are found to result from the combined effect of trigonal distortion and contributions of the symmetry adapted d_{π} -orbitals involved due to coupling with corresponding counterparts from the bidentate ligand (*phase coupling*). The larger splitting of the lowest excited state ${}^2E_g(O_h)$ in the analogous ClO_4^- salt is due to the more distorted geometry of the $[\text{CrN}_6]$ moiety. Related properties of the bipyridine ligand, which turn out to show donor behavior in the present compounds, and the acetylacetonate ligand are discussed, and AOM parameters for the metal–ligand π -interaction are correlated with results of MO calculations.

1. Introduction

The nature of the lowest excited states in chromium(III) complexes has been subject of enormous research efforts by physicists and chemists ever since the detection of the R-lines in ruby by Bequerel.⁴ This exceptional interest is due to the fact that the photochemical and photophysical behavior is controlled by the level sequence of the excited states, which are well known (by experiment and theory) for compounds containing Cr^{3+} chromophores.^{5,6} In the case of $[\text{Cr}(\text{bpy})_3]^{3+}$, bpy = 2,2'-bipyridine, however, the overlap of d–d bands with low-lying charge-transfer bands has so far prevented reliable assignments for the two familiar quartet transitions.⁷ Likewise, information on the low-lying spin-forbidden transitions, ${}^4A_{2g} \rightarrow {}^2E_g, {}^2T_{1g}$, has been poor until recently, when Hauser et al.⁸ reported highly resolved optical spectra of neat crystalline and doped materials. However, their theoretical treatment in terms of the conventional ligand field theory (LFT) did not consider the specific π -bonding effects, which are expected to be large

for complexes with bipyridine ligands.^{9,10} Moreover, the influence of the actual molecular geometry was not explicitly considered. The availability of new X-ray data on $[\text{Cr}(\text{bpy})_3](\text{PF}_6)_3$ ¹¹ prompted us to reinvestigate the energy level scheme in view of the predictions of a more flexible theoretical approach, the angular overlap model (AOM), which takes explicit account of the angular coordination geometry. A further extension, recently introduced into the formalism of the AOM, considers phase relations in extended π -electron systems of chelating ligands. The so-called *phase coupling* effect may also be of importance for the present bpy complex, leading to three-center ligand field contributions to the d -orbital energies.¹² This effect has been successfully applied to acetylacetonate complexes of first-row transition metals.^{1–3} Therefore, it is of interest to see whether the extended AOM is also able to explain the low energy states resulting from the t_{2g}^3 electron configuration for $[\text{Cr}(\text{bpy})_3]^{3+}$, which are fairly well separated from the higher energy charge-transfer states. Particular emphasis will be placed on the detailed assignments of Zeeman transitions. The resulting energy level scheme will be compared with predictions obtained from the conventional and the nonadditive ligand field approach. Finally, we will discuss related properties of the bipyridine and the acetylacetonate ligand and show how the relevant AOM parameters for describing π -bonding properties can be analyzed by considering the π -MO's of ligator molecules.

2. Optical Transitions

The prominent bands (R-lines) separated by 19.5 cm^{-1} in the absorption spectrum of crystalline $[\text{Cr}(\text{bpy})_3](\text{PF}_6)_3$ have been unambiguously identified as the zero-phonon transitions into the trigonal split levels $\bar{E} < 2\bar{A}$ of the octahedral parent state 2E_g .⁸ According to Kramers' theorem, all eigenstates of a

† For parts 1–3 in this series, see refs 1–3.

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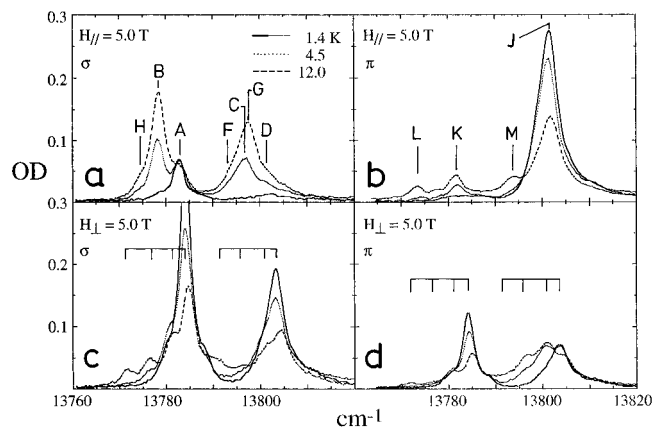


Figure 1. Polarized Zeeman spectra in the region of ${}^4A_{2g} \rightarrow {}^2E_g$ zero-phonon transitions. The capital letters in (parts a and b) refer to Figure 2; the spacings in (parts c and d) are due to the ground state splitting (see text).

Table 1. Electric Dipole Selection Rules for ${}^4A_{2g} \leftrightarrow {}^2E_g$ Transitions in Trigonal d^3 -Systems under the Effect of an External Magnetic Field $H_{||}$ Aligned Parallel to the Molecular C_3 Axis (from Ref 17)

${}^4A_{2g}$	2E_g			
	$\bar{E}_{-1/2}$	$\bar{E}_{+1/2}$	$2\bar{A}_{-1/2}$	$2\bar{A}_{+1/2}$
$\bar{E}_{+1/2}$	$\pi/6$	$\sigma_0/6$	$\sigma_1/12$	$\sigma_0/6$
$\bar{E}_{-1/2}$	$\sigma_0/6$	$\pi/6$	$\sigma_0/6$	$\sigma_1/12$
$2\bar{A}_{+3/2}$		$\sigma_1/4$		$\pi/2$
$2\bar{A}_{-3/2}$	$\sigma_1/4$		$\pi/2$	

system with an odd number of electrons are at least 2-fold degenerate. Therefore, two spin-orbit states of $2\bar{A}$ and \bar{E} symmetry (using the notation of the underlying D_3^* double group) are obtained for the $M_S = \pm 3/2$ and the $M_S = \pm 1/2$ components of the ${}^4A_{2g}$ (O_h) ground state, respectively. Selection rules for the electronic transitions ${}^4A_{2g} \leftrightarrow {}^2E_g$, which are under the regime of a static electric dipole mechanism, are given in Table 1, where σ and π correspond to a light polarization with electric vector perpendicular and parallel to the molecular C_3 axis, respectively. When applied to the transition into the higher $2\bar{A}$ (2E_g) level (R_2), the zero-field splitting (zfs) of the ground state, i.e.

$$D({}^4A_{2g}) = 2\bar{A}_{\pm 3/2}({}^4A_{2g}) - \bar{E}_{\pm 1/2}({}^4A_{2g}) = 2D \quad (1)$$

($2D$ is the zfs parameter commonly used in EPR) can be derived from the slightly different band positions in the polarized absorption spectra: Figure 5a of ref 8 shows the band maximum of R_2 to be shifted by 0.8 cm^{-1} to lower energy in the σ -polarized spectrum reflecting the ordering $2\bar{A} < \bar{E}({}^4A_{2g})$ in accordance with the value of -0.82 cm^{-1} from a Boltzmann analysis.⁸ The zfs of the 2E_g state, which is defined by

$$D({}^2E_g) = 2\bar{A}_{\pm 1/2}({}^2E_g) - \bar{E}_{\pm 1/2}({}^2E_g) \quad (2)$$

is calculated from the separation of R-lines corrected for the zfs of the ground state to $+18.7 \text{ cm}^{-1}$.

An external magnetic field removes Kramers' degeneracies by splitting the states into two components that have opposite values of M_S . Figure 1 shows some highly resolved Zeeman spectra of ${}^4A_{2g} \rightarrow {}^2E_g$ electronic origins in σ - and π -polarization measured at temperatures $T = 1.4, 4.5,$ and 12 K . Although complicated band patterns are obtained by varying temperature and magnetic field, there is a straightforward way for obtaining definite band assignments for all observed spectral features due to zero-phonon transitions. For example, with a magnetic field

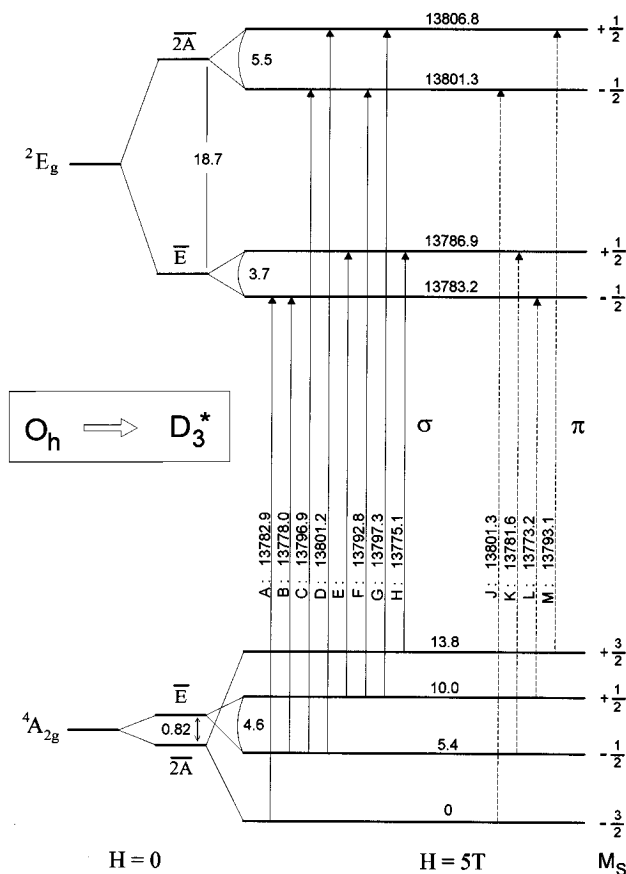


Figure 2. Energy eigenvalues and experimentally obtained transition energies due to the ${}^4A_{2g}, {}^2E_g$ split levels in a magnetic field of $H_{||} = 5 \text{ T}$.

of 5 T applied parallel to the molecular trigonal axis, just one prominent absorption band appears in σ -polarization at $T = 1.4 \text{ K}$ (cf. Figure 1a). At this temperature, only the lowest component of the ground state manifold is populated to any extent. Thus the peak at 13782.9 cm^{-1} , denoted as A, is readily identified as the $2\bar{A}_{-3/2}({}^4A_{2g}) \rightarrow \bar{E}_{-1/2}({}^2E_g)$ transition, since transitions from $2\bar{A}_{-3/2}$ to other states resulting from 2E_g are forbidden in σ . The small features located at 13778.0 (B) and 13796.9 (C) grow rapidly with increasing temperature, showing that these transitions originate from a higher level of the ground state manifold. The comparable band intensities suggest assignments to transitions from $\bar{E}_{-1/2}$ (${}^4A_{2g}$) into $\bar{E}_{-1/2}({}^2E_g)$ and $2\bar{A}_{-1/2}({}^2E_g)$, respectively, both induced by a dipole strength of $\sigma_0/6$ (cf. Table 1). This is confirmed by the related spectrum in π -polarization, which is given in Figure 2b: only one band, denoted as J, appears at $T = 1.4 \text{ K}$, which is readily identified as the $2\bar{A}_{-3/2}({}^4A_{2g}) \rightarrow 2\bar{A}_{-1/2}({}^2E_g)$ transition. The peak position of J, 13801.3 cm^{-1} , should be equal to the energy of $A + C - B$. With a value of 13801.8 cm^{-1} , this is within experimental accuracy.

In π -polarization, selection rules predict three further Zeeman transitions appearing at higher temperatures, and in fact, a total of three bands, K, L, and M, are resolved in the spectrum measured at $T = 12 \text{ K}$. Its temperature behavior proves band K to be a transition originating from the second ground state level, $\bar{E}_{-1/2}({}^4A_{2g})$. According to Table 1, this assignment provides the position of the second component of \bar{E} (2E_g), i.e. $\bar{E}_{+1/2}$. The energy difference 13781.6 cm^{-1} (K) $- 13778.0 \text{ cm}^{-1}$ (B) locates it around 3.5 cm^{-1} higher in energy than $\bar{E}_{-1/2}({}^2E_g)$. This ordering for the split levels of ${}^2E_g(O_h)$ is in accordance with theoretical predictions on the Zeeman splittings

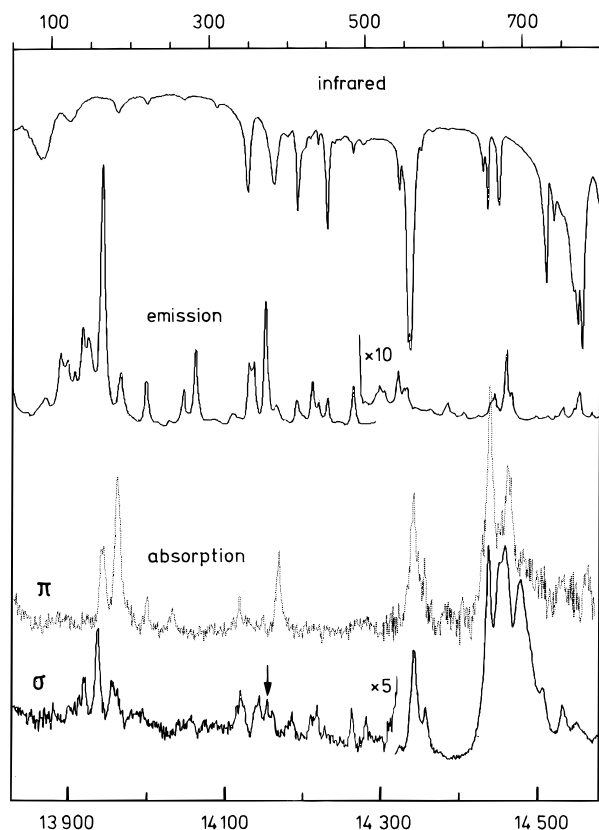


Figure 3. Polarized absorption ($T = 1.4\text{ K}$), emission ($T = 1.4\text{ K}$) and infrared spectra ($T = 10\text{ K}$) in the $50\text{--}800\text{ cm}^{-1}$ region of vibrational transitions. Emission is due to the upper scale using $\nu_{00} - \nu$ with respect to the zero phonon transition $\nu_{00} = 13\,778\text{ cm}^{-1}$ in the $[\text{Rh}]$ doped compound.⁸ The arrow marks the lowest origin of ${}^2\text{T}_{1g}$ in the σ -polarized absorption spectrum (see text and Table 2).

in trigonally distorted chromium(III) compounds.¹³ The energy level diagram showing all electric-dipole allowed ${}^4\text{A}_{2g} \rightarrow {}^2\text{E}_g$ transitions observed for $H_{\parallel} = 5\text{ T}$ is presented in Figure 2. The remaining transitions, D – H, are now easily identified in Figure 1a,b. For example, line L in the π -spectrum corresponds to the $\bar{\text{E}}_{+1/2}({}^4\text{A}_{2g}) \rightarrow \bar{\text{E}}_{-1/2}({}^2\text{E}_g)$ transition as it picks up intensity only at $T = 12\text{ K}$. This assignment determines the Zeeman splitting of $\bar{\text{E}}({}^4\text{A}_{2g})$ to be 4.6 cm^{-1} from the energy difference B – L, as expected with $g_{\parallel}({}^4\text{A}_{2g}) = 1.986$.⁸

The effect of a magnetic field perpendicular to the trigonal axis on the absorption band pattern is shown in Figure 1c,d. Here only the ground state splitting is resolved in either polarization, showing analogous level sequences over ~ 13 wavenumbers as indicated by arrows in the figures. There is in fact no indication of any sizable Zeeman-splitting in the excited state; consequently, the value for g_{\perp} must be close to zero for both Kramers' doublets resulting from ${}^2\text{E}_g$.

Transitions into states which derive from ${}^2\text{T}_{1g}(O_h)$ are expected a few hundred wavenumbers higher in energy. Figure 3 shows the σ - and π -polarized absorption bands in the region $13\,800\text{--}14\,600\text{ cm}^{-1}$ together with related transitions obtained from low-temperature emission and infrared measurements. Locating further electronic origins is complicated by the fact that almost all observed peaks can be identified with vibrational sidebands of one of the origins of ${}^2\text{E}_g$. Table 2 collects the respective assignments showing only the $14\,034$ and $14\,160\text{ cm}^{-1}$ lines having no counterpart in the emission or infrared spectrum. We assign the higher band (arrow in Figure 3) to the lowest spin-orbit component of ${}^2\text{T}_{1g}$, which turned out to

Table 2. Vibronic Zero-Field Transitions in the Low-Temperature Absorption Spectrum and Related Vibrational Frequencies Observed in Emission^a and Infrared Spectra

ν	absorption		emission $\nu_{00} - \nu$	infrared
	ν	$\nu - \nu_{00}$		
	$\nu = 13778$ (σ) origin: $\bar{2}\text{A}({}^4\text{A}_{2g}) \leftrightarrow \bar{\text{E}}({}^2\text{E}_g)$			
	$\nu = 13797$ (π) origin: $\bar{2}\text{A}({}^4\text{A}_{2g}) \leftrightarrow \bar{2}\text{A}({}^2\text{E}_g)$			
13925		129	129	125
13943	165	164	164	
13961				
13961	183		186	184
14000	222		221	221
14034	?			
14126	348		352	351
14148		351		
14160	(origin)			
14169	382		386	384
14189		382		
14191	413		412	414
14211		414		
14219	441		439	440
14263	484		486	485
14281		484		
14322	544		536	544
14341		544		
14333	555		550	555
14352		555		
14337	559			559
14356		559		
14349	571		570	571
14368		571		
14429	651		651	651 m
14448		651		
14435	657		664	657 s
14454		657		
14449	671		670	671 s
14468		671		
14507	729			729 w
14526		729		
14510	732		733	732 s
14529		732		
14520	742			742 m
14539		742		
14556	778		779	778
14807	1029	1010		1016, 1023
14829	1051	1032		1036
15296	1516			1520

^a From the unpolarized emission spectrum of $[\text{Rh}(\text{bpy})_3](\text{PF}_6)_3 \cdot \text{Cr}^{3+}$ at $T = 1.4\text{ K}$; $\nu_{00} = 13\,777\text{ cm}^{-1}$.

be of $\bar{\text{E}}$ symmetry (see below) according to its polarization behavior of σ -type for the corresponding low-temperature transition $\bar{2}\text{A}({}^4\text{A}_{2g}) \rightarrow \bar{\text{E}}({}^2\text{T}_{1g})$. The other two zero-phonon transitions into the trigonally split levels of ${}^2\text{T}_{1g}$ may be located around $14\,450\text{ cm}^{-1}$ for the following reasons: (i) a Gaussian band deconvolution of the broad absorption shape shows some additional weak transitions here, which are covered under the intense vibrational sidebands (due to the prominent 657 and 671 cm^{-1} modes) upon both electronic origins; (ii) applying a magnetic field perpendicular to the C_3 axis leads to surprisingly high intensities at $14\,440\text{ cm}^{-1}$ and, less pronounced, at $14\,465\text{ cm}^{-1}$, which is illustrated in Figure 9 of ref 8. This increase of intensity for some spin-forbidden transitions may be explained by Zeeman-induced mixing of the doublet states involved with components of close-lying quartet states (either d^3 or charge transfer). The latter give rise to more intense spin-allowed transitions.²³

In the region of ${}^4\text{A}_{2g} \rightarrow {}^2\text{T}_{2g}(O_h)$ transition a series of prominent lines has been observed in the polarized absorption spectra (*cf.* Figure 4 in ref 8). The first sharp band located at

19 999 cm^{-1} is of $\overline{2A}$ character as calculated for the lowest spin-orbit component of ${}^2T_{2g}$ (see below). Therefore it is plausible to assign this band as the respective electronic origin, which causes several vibronic satellites with vibrational energies of 155, 167, 372, 665, and 768 cm^{-1} . The most intense peak in σ -polarization is located at 20 056 cm^{-1} and may also be assigned to a doublet origin, because sidebands appear at similar frequencies (155, 372, 665 cm^{-1}). The peaks at 20 488 and 20 650 cm^{-1} , defying assignments to vibronic sidebands of either origin, are candidates for the third spin-orbit component of ${}^2T_{2g}$. However, since we are finally not able to distinguish between the zero-phonon transitions of doublet, quartet (${}^4A_{2g} \rightarrow {}^4T_{2g}$) or low-lying charge transfer states, which also appear in this spectral region, these assignments cannot be established by spectroscopic arguments alone.

3. AOM Calculations

As described in detail by Ceulemans et al.,¹² Atanasov et al.,¹ and Schäffer and Yamatera,¹⁴ *nonadditive* contributions to the ligand field potential may occur in complexes with chelate ligands which have an extended π -electron system. Within the framework of the conventional (*additive*) AOM, the energy matrix for the π -orbitals contains two antibonding parameters, which describe the π -interaction in the chelate plane by $e_{\pi c}$ (or $e_{\pi||}$) and perpendicular to it by $e_{\pi s}$ (or $e_{\pi\perp}$). Following Orgel,¹⁵ this description is not valid when delocalized π -electrons are involved as, for example, in acetylacetonate or bipyridyl ligands.¹² Considering the respective $\overline{L-M-L}$ moiety, the relevant molecular orbitals can be classified with respect to the C_2 axis into symmetric (χ -type) or antisymmetric (ψ -type) MO's. Since combination with metal d-functions can take place only within the same symmetry, wave functions have to be transformed to the relevant C_{2v} symmetry to become adequate linear combinations of the usual basis functions:

$$\begin{aligned} b_1: & \quad d_{\psi} = \sqrt{1/2}(d_{xz} + d_{yz}) \\ a_2: & \quad d_{\chi} = \sqrt{1/2}(d_{xz} - d_{yz}) \end{aligned} \quad (3)$$

Within this approach, two different π -parameters describe the out-of-plane interactions between in-phase ψ -type ($e_{\pi s}$) and out-of-phase χ -type ($e_{\pi c}$) metal and ligand orbitals, respectively. These quantities will certainly be dependent on the respective MO energies of the free ligand which are generally different for ψ - and χ -type wave functions. The contributions of the HOMO for π -donor ligands and for the LUMO for π -acceptor ligands are usually the most important because of the small energy denominators associated with these molecular orbitals. However, consideration of all individual contributions of filled and empty ligand orbitals may be required in some cases (*vide infra*).

AOM calculations have been performed by diagonalizing the full 120×120 secular determinant of the d^3 system. The underlying AOM matrix for trigonal $M(L-L)_3$ complexes of D_3 symmetry, which is supplemented for orbital phase coupling effects, has been published previously.³ This matrix was implemented into the AOMX program allowing full account of electronic repulsion, spin-orbit coupling, and Zeeman level splittings for arbitrary d^n complexes.¹⁶

4. Orbital Scheme and Ligand Field States

Ligand field calculations on $[\text{Cr}(\text{bpy})_3]^{3+}$ have already been performed by Hauser et al.⁸ and, in terms of an extended angular overlap model, by Hoggard and Lee.¹⁰ These calculations have required a total of six parameters, which may be varied independently: the Racah parameters B and C , the spin-orbit coupling parameter ζ , and three ligand field quantities (Dq , K , K') or AOM parameters (e_{σ} , $e_{\pi s}$, $e_{\pi c}$), respectively. However, the appearance of low-lying charge transfer bands, which cover the quartet and higher doublet transitions, strongly confine the experimental data basis, confronting us with the problem of overparameterization which can lead to a good fit even for incorrect assignments. Therefore, we begin with a more qualitative discussion, placing the emphasis on relevant geometries and orbital schemes in order to elucidate the physical origins of the measured band splittings.

The polarized optical spectra of $[\text{Cr}(\text{bpy})_3](\text{PF}_6)_3$ and their changes with magnetic field and temperature variation determine the level ordering for the zfs of the quartet ground state and the first excited doublet state (*cf.* eqs 1 and 2):

$${}^4A_{2g}(O_h): \quad \overline{2A} < \overline{E}; D({}^4A_{2g}) = -0.82 \text{ cm}^{-1} \quad (4)$$

$${}^2E_g(O_h): \quad \overline{E} < \overline{2A}; D({}^2E_g) = +18.7 \text{ cm}^{-1} \quad (5)$$

As has been shown previously, the ground state zfs in a trischelated $[\text{Cr}(L-L)_3]$ compound is predominantly influenced by the trigonal distortion from the O_h geometry rather than by the distinct π -interaction with either acceptor- or donor-type ligands.^{3,13} The theoretical ${}^4A_{2g}$ sublevel sequence $\overline{2A} < \overline{E}$ ($\overline{E} < \overline{2A}$) was found to be correlated with a trigonally compressed (elongated) geometry. This is reflected by the experimental data for the present compound. The particularly large zero-field splitting of $\sim 0.8 \text{ cm}^{-1}$ together with the sequence of the split levels (eq 1) is in agreement with a trigonal compression of the $[\text{CrN}_6]$ octahedron by a large deviation of the polar angle $\vartheta = 58^\circ$ from the value for cubic symmetry ($\vartheta_{\text{cub}} = 54.74^\circ$).¹⁰

Information on the 2E_g splitting in trigonally distorted d^3 complexes, on the other hand, can be obtained from the familiar relation¹⁷

$$D({}^2E_g) = \overline{2A}({}^2E_g) - \overline{E}({}^2E_g) = \frac{4}{3}\zeta \frac{\Delta t_2}{{}^2E_g - {}^2T_{2g}} \quad (6)$$

where Δt_2 represents the energy difference between the e-type and a_1 -type t_{2g} -orbitals in a trigonal ligand field. (It should be noted that the effect of mixing $e(t_{2g})$ and $e(e_g)$ orbitals is originally not considered in the definition of Δt_2 .¹³) Combining eqs 5 and 6 implies that Δt_2 must be negative to explain the measured sequence of the 2E_g split levels. We will now attempt to elucidate in which way this result is influenced by the specific π -interaction with the bipyridine ligand. As illustrated in Figure 4, the HOMO (LUMO) of bpy is given by an out-of-phase (in-phase) combination of the ligator π -MO's. Since this phase relation is opposite compared to the frontier orbitals of the acetylacetonate ligand, it was suggested that the inverted 2E_g splitting of $[\text{Cr}(\text{bpy})_3]^{3+}$ with respect to $[\text{Cr}(\text{acac})_3]$ is just the result of this difference.⁹ However, this effect may be modified by the large trigonal distortion of the $[\text{CrN}_6]$ chromophore in $[\text{Cr}(\text{bpy})_3]^{3+}$, which contributes considerably to Δt_2 as well. In order to separate the geometric effect (trigonal distortion) from electronic properties (in-phase or out-of-phase π -interaction,

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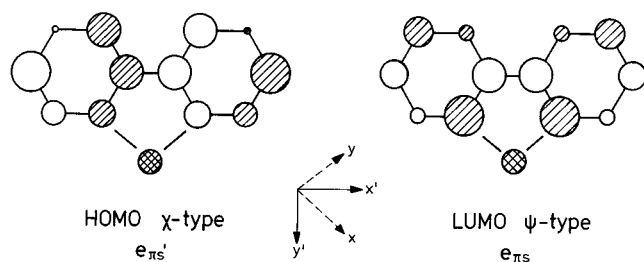


Figure 4. Out-of-phase type HOMO and in-phase type LUMO orbitals of bipyridine which are symmetric (a_2) and antisymmetric (b_1) with respect to the C_2 axis.

donor or acceptor behavior), the energy level scheme of the metal d-orbitals is considered first. In a sample calculation, we therefore allowed for positive and negative values of a mean parameter, i.e. $\bar{e}_{\pi s} = (1/2)(e_{\pi s} + e_{\pi s}')$, implying overall donor and acceptor character, respectively, and we examined both types of phase coupling by varying $de_{\pi s} (=e_{\pi s} - e_{\pi s}')$, including the possibility of no phase coupling ($e_{\pi s} = e_{\pi s}'$). Figure 5a shows the energy splittings of the t_{2g} -orbitals, Δt_2 , in a contour diagram with $\bar{e}_{\pi s}$ and $de_{\pi s}$ as variables and the other parameters fixed at reasonable values. The experimental value of $D(^2E_g)$, requiring $\Delta t_2 < 0$, immediately excludes in-phase coupling with donor behavior. But the experimental findings can still be qualitatively reproduced by assuming either out-of-phase coupling and overall donor or acceptor properties, or in-phase coupling and overall acceptor character. A π -acceptor interaction with no phase coupling does also not violate the correct orbital sequence. This is due to the fact that a trigonal compression of the $[\text{CrN}_6]$ polyhedron gives a negative contribution for acceptor properties but may result in a positive contribution to Δt_2 for donor properties of the bpy ligand (Figure 5b).

We have performed a series of AOM calculations on the full d^3 system of $[\text{Cr}(\text{bpy})_3]^{3+}$. The structural parameters involved, i.e. the angular geometry of the chromophore and the orientations of the chelate planes as given by the angle ψ ,³ were taken from refs 11 and 18 for the PF_6^- and the ClO_4^- salts, respectively. Comparison with the experiment was limited to the energy levels originating from the t_{2g}^3 electron configuration, because transitions to other states are hidden in the absorption spectrum under very intense charge transfer bands. Our calculations show the splittings of 2E_g and $^2T_{1g}$ to be predominantly influenced by the spin-orbit coupling (ζ) and by the out-of-plane π -interaction ($\bar{e}_{\pi s}$ and $de_{\pi s}$). In the following ζ is set to 200 cm^{-1} as estimated from EPR measurements on $[\text{Rh}(\text{bpy})_3](\text{PF}_6)_3:\text{Cr}^{3+}$,⁸ and the model parameters B , e_σ and $e_{\pi c}$ are fixed at values known from the AOM analysis of the related pyridine complex.¹⁹ This leaves us with the Racah parameter C , which can be adjusted to fit the absolute doublet energies, and $e_{\pi s}$ and $e_{\pi s}'$ as variables. A least-squares fitting procedure based on the Powell algorithm⁵ reproduces the experimental energies of 2E_g and $^2T_{1g}$ states (*cf.* section 2) pretty well in terms of negative e_π parameters ($\bar{e}_{\pi s} < 0$) and $de_{\pi s}$ close to zero (no phase coupling). This result, which is presented in Table 3, seems in accordance with the alleged π -acceptor character of the bpy ligand.^{9,10} However, since $D(^2E_g)$ is proportional to Δt_2 , there is not just one set of parameters $\bar{e}_{\pi s}$ and $de_{\pi s}$ which reproduces the experimental value of $\sim 19 \text{ cm}^{-1}$. This is demonstrated by comparing Figure 5a with a contour plot, which shows a number of isolines for the calculated splittings of 2E_g including the isoline relevant for the spectroscopic findings (Figure 6).

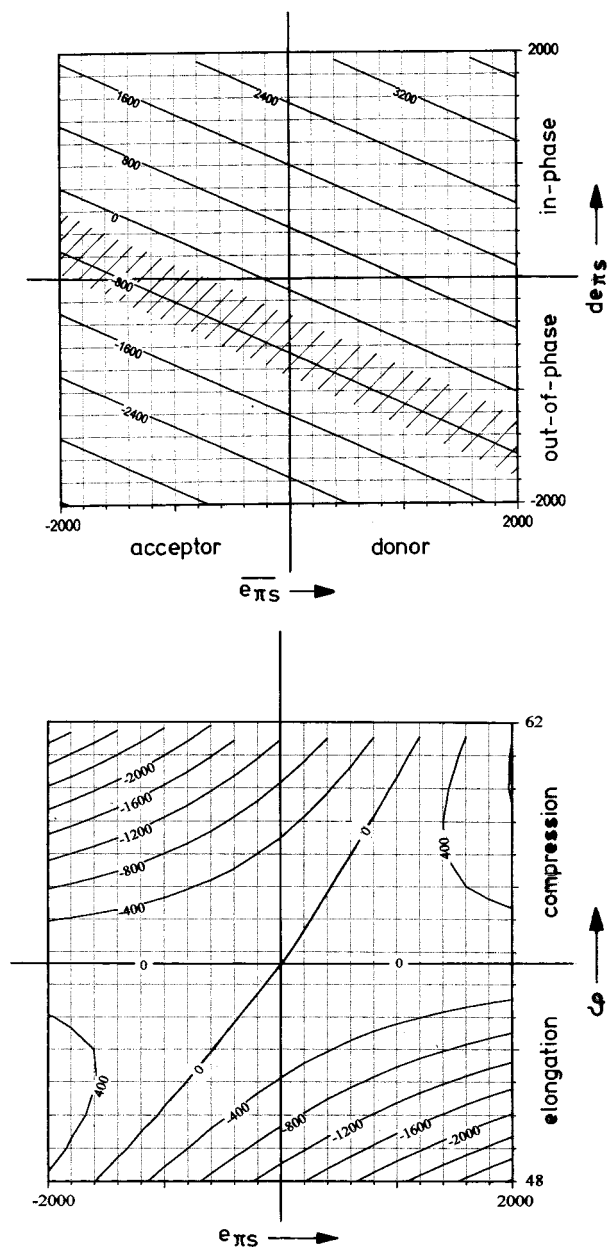


Figure 5. Top (a): Contour plot for the t_{2g} -orbital splitting of the PF_6^- salt due to the π -contributions perpendicular to the planes of the bpy ligands. The splitting calculated from eq 6 is within the marked area ($e_\sigma = 8000 \text{ cm}^{-1}$, $\vartheta = 58^\circ$, $\phi = 49.2^\circ$). Bottom (b): Analogous plot with respect to the effect of trigonal distortions versus the (isotropic) π -behavior of the chromium-bipyridine interaction ($e_\sigma = 8000 \text{ cm}^{-1}$, $\phi = 60^\circ$).

The situation is somewhat different for the ClO_4^- salt, where the molecular geometry of the $[\text{Cr}(\text{bpy})_3]^{3+}$ chromophore is much more distorted than for the PF_6^- salt.¹⁸ In accordance with this geometric effect, the 2E_g splitting appears to be distinctly larger (95 cm^{-1} or less) than for the PF_6^- salt (we prefer an alternative interpretation of the excitation spectrum given in ref 18, where the 2E_g splitting is claimed to be $\sim 165 \text{ cm}^{-1}$). Figure 6 includes isolines for the 2E_g splitting as a function of $\bar{e}_{\pi s}$ and $de_{\pi s}$ using the structural data for the ClO_4^- salt from ref 18. Assuming that these parameters are the same for both salts, i.e. that the differences in $D(^2E_g)$ are due to geometric impacts only, $\bar{e}_{\pi s}$ and $de_{\pi s}$ should be determined by the crossing point of the $D(^2E_g) = 19 \text{ cm}^{-1}$ isoline in the PF_6^- salt and the respective isoline of the ClO_4^- salt⁸ (probably for the value of 95 cm^{-1}). However, we are not able to clarify the role of π -bonding by this procedure yet, because there are two

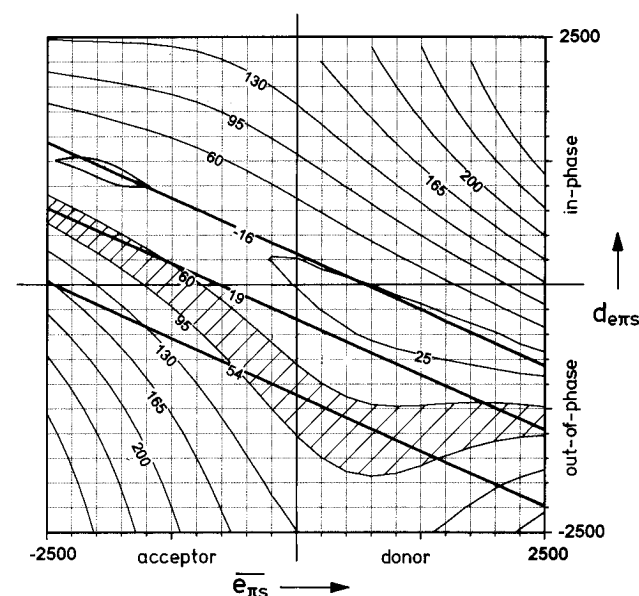
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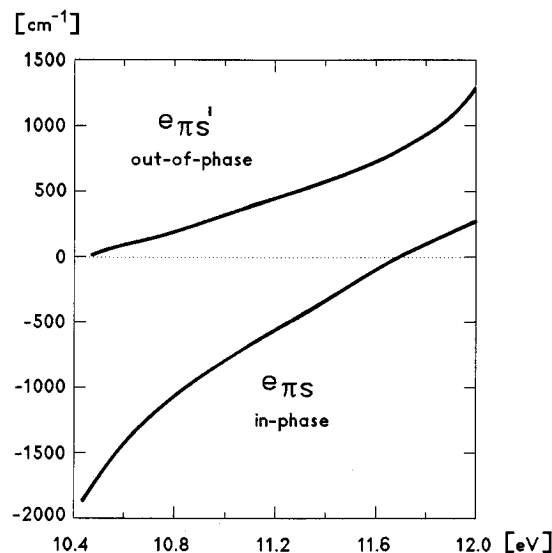
Table 3. Observed and Calculated d-d Transition Energies in [Cr(bpy)](PF₆)₃ with Parameter Values Fixed^a ($e_{\sigma} = 8000$, $e_{\pi c} = 0$, $B = 600$, $\zeta = 200$) and All Data Given in cm⁻¹

assignments		observed ^b	calculated	
			<i>a</i>	<i>b</i>
⁴ A _{2g}	$\overline{2A}$	0	0	0
	\overline{E}	0.83	0.54	0.62
	<i>2D</i>	+0.83	+0.54	+0.62
² E _g	\overline{E}	13 778	13 785	13 776
	$\overline{2A}$	13 797	13 805	13 795
	<i>D</i>	+19	+20	+19
² T _{1g}	\overline{E}	14 160	14 138	14 133
	$\overline{2A}$	14 437	14 442	14 472
	\overline{E}	14 461	14 451	14 483
	<i>D</i>	301	313	350
² T _{2g}	$\overline{2A}$	19 999	21 538	21 156
	\overline{E}	20 056 ^c	21 638	21 211
	\overline{E}	20 488 ^c	22 180	21 526
	<i>D</i>	489	642	370
fitted param ^a			π -acceptor ^d	π -donor ^e
$e_{\pi s}$			-950	500
$e_{\pi s'}$			-1000	1250
<i>C</i>			3080	3100

^a See text. ^b From ref 8. ^c Tentative assignment. ^d $\overline{e_{\pi s}} = -975$, $de_{\pi s} = 50$ (i.e. almost no phase coupling). ^e $e_{\pi s} = 875$, $de_{\pi s} = -750$ (i.e. out-of-phase coupling).

**Figure 6.** Isolines for the energy separation of the ²E_g split levels in the trigonal PF₆⁻ compound (bold lines) and in the low-symmetry ClO₄⁻ compound. The experimental values are given with the 19cm⁻¹ isoline (PF₆⁻ salt) and in the case of the perchlorate salt by the marked area (uncertain assignment). Other parameters are as in Table 3.

well-suited areas in the parameter space exhibiting rather opposite parameter values. Despite the fact that the solution showing strong acceptor behavior ($\overline{e_{\pi s}} < 0$) resembles the analysis of Hoggard,¹⁰ it will be disregarded on the basis of our EHT-MO calculations (*cf.* section 6). Another possibility presents itself in the region of donor properties and dominating out-of-phase coupling. This solution ($\overline{e_{\pi s}} > 0$, $de_{\pi s} < 0$) is also consistent with the parameters obtained when all observed transition energies are fitted simultaneously. Table 3 compares the experimental transition energies of the low-lying d-states of [Cr(bpy)₃](PF₆)₃ with the level schemes calculated on the basis of optimized parameters for the metal–ligand π -interac-

**Figure 7.** Calculated values of the π -interaction parameters for [Cr(bpy)₃]³⁺ as a function of the free d-orbital energy (*see text*).**Table 4.** g_{\parallel} Values of ²E_g Sublevels and ²E_g Splitting Calculated under the Influence of Orbital Expansion ($k < 1$) and Trees' Correction ($\alpha > 0$)^a

Part a					
	expt	calculated			
		$k = 1$	$k = 0.8$	$k = 0.6$	$k = 0.4$
$g_{\parallel}(\overline{2A})$	≈2.4	0.8	1.1	1.3	1.5
$g_{\parallel}(\overline{E})$	≈1.6	3.0	2.9	2.6	2.4
<i>D</i> (² E _g)	19	19	15	11	8
Part b					
	expt	calculated			
		$\alpha = 0$	$\alpha = 100$	$\alpha = 200$	$\alpha = 300$
$g_{\parallel}(\overline{2A})$	≈2.4	0.8	1.1	1.6	2.3
$g_{\parallel}(\overline{E})$	≈1.6	3.0	2.8	2.5	2.1
<i>D</i> (² E _g)	19	19	27	32	29
² T _{2g} – ² E _g	6400	7500	7150	6800	6450

^a The energy separation of ²T_{2g} and ²E_g, given also in Part b, is not dependent on k . Other parameters as for Table 3. All in cm⁻¹.

tion. Because there is good agreement with the experimental results in either case, we are unable to characterize the π -bonding behavior at the present stage.

5. Zeeman Splittings

Further insight into the π -bonding scheme may be obtained by considering the Zeeman splitting of ⁴A_{2g} and ²E_g states. Applying the Zeeman operator of the form¹⁷

$$\mathbf{H}_{\text{mag}} = \beta H \{ \sin \vartheta_{\text{mag}} \cos \varphi_{\text{mag}} (k_x L_x + 2S_x) + \sin \vartheta_{\text{mag}} \sin \varphi_{\text{mag}} (k_y L_y + 2S_y) + \cos \vartheta_{\text{mag}} (k_z L_z + 2S_z) \} \quad (7)$$

to the real basis functions of d³, values for g_{\perp} and g_{\parallel} were calculated for each electronic state using the following relation ($\beta = 0.4668 \text{ cm}^{-1} \text{ T}^{-1}$)

$$g_{\perp(l)} = \Delta E_{\perp(l)} / \beta H_{\perp(l)} \quad (8)$$

The Zeeman splittings show, as expected, much larger effects for the magnetic field aligned parallel to the trigonal axis. For a magnetic field of $H_{\parallel} = 5 \text{ T}$ the same level sequence of ²E_g split components (defined by pseudo-spin values $-1/2$, $+1/2$) is

Table 5. π -Type MO Energies and Their Composition from Iterative Extended Hückel Calculations on $[\text{Cr}(\text{bpy})_3]^{3+a}$

no.	energy		type		MO coefficients	
1	-2.158		χ		0.999 ϕ_1	
2	-4.398	-2.185	ψ	ϕ_1	0.495 $4p_z$ + 0.878 ϕ_2 - 0.131 ϕ_6	-0.323 (p_{z1} - p_{z2}) + ...
3	-5.882	-4.803	ψ	ϕ_2	-0.837 $4p_z$ + 0.478 ϕ_2 - 0.140 ϕ_5 + 0.269 ϕ_6	+0.289 (p_{z1} + p_{z2}) + ...
4	-6.664	-6.430	χ	4p	-0.130 ϕ_{10} - 0.142 ϕ_{12} - 0.042 $d_{y'z'}$	+1.0 $4p_z$
5	-8.404	-6.665	χ	ϕ_3	1.0 ϕ_3	-0.022 (p_{z1} - p_{z2}) + ...
6	-8.480	-8.452	ψ	ϕ_4	0.107 $d_{x'z'}$ + 0.997 ϕ_4	-0.364 (p_{z1} - p_{z2}) + ...
7	-8.476	-8.455	ψ	ϕ_5	0.053 $d_{y'z'}$ + 0.987 ϕ_5	+0.142 (p_{z1} + p_{z2}) + ...
8	-9.476	-9.349	ψ	ϕ_6	0.162 $d_{y'z'}$ - 0.944 ϕ_6	+0.426 (p_{z1} + p_{z2}) + ...
9	-12.415	-12.700	χ	3d	0.750 $d_{x'z'}$ - 0.632 ϕ_7 - 0.214 ϕ_9 - 0.140 ϕ_{11}	1.0 $d_{x'z'}$
10	-12.530	-12.700	ψ	3d	-0.944 $d_{y'z'}$ - 0.128 ϕ_6 + 0.081 ϕ_8	1.0 $d_{y'z'}$
11	-12.669	-12.572	χ	ϕ_7	-0.299 ϕ_{10} - 0.156 ϕ_{12}	+0.140 (p_{z1} - p_{z2}) + ...
12	-13.701	-13.697	ψ	ϕ_8	-0.590 $d_{x'z'}$ - 0.774 ϕ_7 + 0.204 ϕ_9	+0.039 (p_{z1} + p_{z2}) + ...
13	-13.809	-13.725	χ	ϕ_9	+0.117 ϕ_{11}	+0.324 (p_{z1} - p_{z2}) + ...
14	-14.008	-13.869	ψ	ϕ_{10}	0.993 ϕ_8 + 0.108 ϕ_{10}	-0.347 (p_{z1} + p_{z2}) + ...
15	-15.398	-15.347	χ	ϕ_{11}	0.252 $d_{x'z'}$ + 0.956 ϕ_9	-0.436 (p_{z1} - p_{z2}) + ...
	-16.056	-16.004	ψ	ϕ_{12}	-0.260 $d_{y'z'}$ + 0.940 ϕ_{10}	+0.369 (p_{z1} + p_{z2}) + ...
					-0.136 $d_{x'z'}$ - 0.982 ϕ_{11}	
					-0.108 $d_{y'z'}$ + 0.981 ϕ_{12}	

^a The second lines refer to the orbitals of Cr^{3+} and 2,2'-bipyridine (denoted by $\phi_i = 1, \dots, 12$) without metal-ligand interaction. Coordinate system choice as given in Figure 4. Only MO-coefficients for d- and p-orbitals of the metal, and for π -orbitals of ligand atoms are presented. Cr orbital exponents: $4s = 4p, 1.70$; $3d, 4.95 (0.50579) + 1.80 (0.67472)$. Orbital energies (in eV): input $H_{4s} = -8.66, H_{4p} = -5.24, H_{3d} = -11.22$. Output after charge iteration: $H_{4s} = -10.271, H_{4p} = -6.43, H_{3d} = -12.696$. Iterated configuration of Cr: $4s^{0.360}4p^{0.216}3d^{4.88}$.

calculated as predicted from the spectroscopic assignments. On the other hand, Zeeman splittings of $\bar{E}(^2E_g)$ and $2\bar{A}(^2E_g)$ are calculated to be rather small (1.3 and 0.4 cm^{-1} , respectively) when a magnetic field perpendicular to the trigonal axis is applied. This is again in line with the experiment showing Zeeman splittings spectroscopically not resolved in any case for $H_{\perp} = 5$ T.

However, the calculated g_{\parallel} values are significantly different for \bar{E} ($g_{\parallel} = 3$) and $2\bar{A}$ ($g_{\parallel} = 0.9$) compared to values of ~ 1.6 and ~ 2.4 , respectively, derived from the absorption spectra. In accordance with our experimental result, Riesen reported $g_{\parallel} = 1.76 \pm 0.01$ for the lowest excited state, $\bar{E}(^2E_g)$, from fluorescence line-narrowing measurements.²⁰ On the other hand, the AOM calculations on g_{\parallel} can be somewhat improved if the Stevens orbital reduction ($k < 1$)²¹ and Trees' correction ($\alpha > 0$)⁵ are taken into account. Both effects lower $g_{\parallel}(\bar{E})$ and increase $g_{\parallel}(2\bar{A})$ correspondingly as illustrated by the data in Table 4.

6. Nature of the Metal-Ligand π -Bonding

In this section we discuss the various contributions to the π -bonding parameters derived for the bipyridine complex, and compare them with the recently investigated acetylacetonate complex of chromium(III). For this purpose the perturbation

on the metal-centered d_{π} -orbitals by the π -type MO's of bipyridine is explicitly considered. The latter can be divided into occupied (donor) and non-occupied (acceptor) MO's, giving positive and negative contributions to the energies of the corresponding metal functions, respectively. The other classification of these orbitals is given by in- and out-of-phase symmetry properties influencing $e_{\pi s}$ and $e_{\pi s}'$ separately. Therefore, making use of symmetry-adapted d-orbitals (cf. Figure 4), we have to consider in total four terms contributing to the out-of-plane metal-ligand π -interaction:

$$\text{in-phase: } e_{\pi s}(d_{y'z'}) = e_{\pi s}(\text{donor}) + e_{\pi s}(\text{acceptor})$$

$$\text{out-of-phase: } e_{\pi s}'(d_{x'z'}) = e_{\pi s}'(\text{donor}) + e_{\pi s}'(\text{acceptor}) \quad (9)$$

The various terms in eq 9 were obtained from a second-order perturbation, using expressions for each of the four possible combinations, which are given, for example, by

$$e_{\pi s}(\text{donor}) = 2H_{p-d\pi} \sum_{li} c_{li}^2 / (H_d - H_l) \quad (10)$$

Here c_{li} is the MO coefficient of the ligand $2p_z$ -orbital ($i = 1, 2$) in the corresponding π -type ligand MO (l numerates the in-phase orbitals only), and $(H_d - H_l)$ represents the energy difference between the 3d-orbitals of Cr^{3+} and that MO. Numerical values were evaluated by a standard extended Hückel calculation,²² where the resonance integral $H_{p-d\pi}$ was set to 0.738 eV using the Wolfsberg-Helmholz approximation. The calculated values of $e_{\pi s}$ and $e_{\pi s}'$ are plotted in Figure 7 as function of the d-orbital energy H_d .

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The analysis of the various contributions to the π -interaction show that the energy effect of the ligand p-orbitals on the corresponding metal d-orbitals cannot be due to interactions of HOMO and/or LUMO type alone. In fact, ligand orbitals which are more distant in energy have to contribute considerably to the π -parameters, i.e. to the ligand field potential acting on the Cr^{3+} ion. Figure 7 shows that the overall π -bonding function of bpy varies from acceptor to donor depending on the explicit value of H_d . This means that contributions of the π -functions of bpy crucially depend on the position of the metal d-orbitals with respect to the ligand ones. Iterative extended Hückel calculations for the Cr-bpy moiety show that the assumed standard energy $H_d = -11.22$ eV drops on charge iteration to -12.955 eV, approaching the HOMO's of the ligand. The respective MO energies and coefficients as well as input and output parameter values are given in Table 5. The MO's orbitals of mainly metal-d character (nos. 8, 9: d_x , d_y) are affected mostly by occupied ligand π -orbitals. As seen from the d-contributions to the MO's of dominant ligand character, d_x is primarily influenced by HOMO no. 10, while d_y undergoes most perturbation from a lower lying ψ type ligand orbital (no. 13). The EHT calculations thus corroborate the postulated donor properties with dominant out-of-phase π -interaction, i.e. and $e_{\pi s}' > e_{\pi s} > 0$. It is also seen from the MO's in Table 5 that d_x shows a larger covalent reduction than d_y , which correlates with the a_1 - and e-type orbitals in the tris-chelated complex.¹ This could serve as explanation for covalent orbital reduction factors $k_z < k_{x,y}$ as well as for orbital quenching by introducing Trees' correction which result from the fitting of the trigonal level splittings in magnetic fields (*cf.* Table 4).

In summary, the bpy ligand was found to act as an out-of-phase π -donor ligand to Cr^{3+} , where the metal-ligand π -interactions are determined also by more distant energy levels which contribute by means of some larger MO-coefficients, overcompensating the energy denominator in eq 10. This situation has not been explicitly considered for the earlier investigated complex $[\text{Cr}(\text{acac})_3]$, where perturbation on the d_π -levels only by virtue of its HOMO (donor function) have been used in order to explain the energy level scheme.^{1,9} Thus we have to check our approximation by using all Hückel MO's of the acac ligand, likewise. Neglecting in first approximation the difference between the carbon and oxygen atoms, the energies for the π -MO's (in terms of Hückel's parameter $\beta < 0$) and MO-coefficients for the frontier ligand orbitals are readily obtained. Taking the ligand p-orbital energy at zero (O-atom)

and denoting the Cr-3d energy by Δ , we calculate the π -parameters $e_{\pi s}$ and $e_{\pi s}'$ (and the related values of $e_{\pi s}$ and $de_{\pi s}$) as

$$\begin{aligned} e_{\pi s}(\text{donor}) &= 2H_{p-d\pi}^2 \{ \frac{1}{3}\Delta + 1/[12(\Delta + \sqrt{3}|\beta|)] \} \\ e_{\pi s}'(\text{donor}) &= 2H_{p-d\pi}^2 / \{ 4(\Delta + |\beta|) \} \\ e_{\pi s}(\text{acceptor}) &= 2H_{p-d\pi}^2 / \{ 12(\Delta - \sqrt{3}|\beta|) \} \\ e_{\pi s}'(\text{acceptor}) &= 2H_{p-d\pi}^2 / \{ 4(\Delta - |\beta|) \} \end{aligned} \quad (11)$$

Experimental data show that the ligand-to-metal charge-transfer transitions are at far lower energy than the ligand-ligand transitions, implying $\Delta \ll |\beta|$. Therefore $e_{\pi s}(\text{donor})$ clearly dominates, followed by a smaller $e_{\pi s}'(\text{acceptor})$ interaction. In this respect the acac ligand, which causes in-phase perturbation on the d_π -levels mainly by virtue of its HOMO, can be considered as a rather limiting case. This result is not changed, in fact, when better acac orbitals, e.g. obtained from ab initio calculations, are used.¹

7. Conclusion

The present investigation illustrates that the trigonal level splittings in tris-chelated chromium(III) complexes, as far as reliable experimental data are available, can be rationalized and elucidated within the angular overlap model when symmetry and energy effects of the ligand π -electrons on the d-levels are appropriately considered. Although low-lying charge transfer states influencing the latter in an unknown way limit applications of the ligand field model, in particular with respect to the numeric accuracy of the calculated energies, the phase coupling concept developed within the AOM approach is shown to be a useful guide to account for extended π -effects, while preserving the attractive features of the ligand field description.

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